## Errata for Elementary Differential Geometry, 2nd Edition by O'Neill

## Chapter 1:

## Page/Line Correction

15/4 missing period after "differentiation".
$15 / 7 \quad$ In $y^{2} U_{3}\left[x^{2} y\right]$ the $y^{2} U_{3}$ should be italicized.
15/-6 Should read $V\left[x_{i}\right] U_{i}$ (subscript "i").
24/-8 Should read $\mathbf{R}^{3}$, not $\mathbf{R}^{2}$, and $f_{i}=\phi\left(U_{i}\right)$, not $f_{t}=\phi\left(U_{i}\right)$
26/-2 Should read $\ldots=x U_{1}$ (subscript " 1 ").
$32 / 11 \quad$ Should read $r, \vartheta, z$, not $r, \phi, z$
$36 /-1 \quad$ Should read $\ldots=\mathbf{v}\left[f_{i}\right]$, not $\mathbf{v}[f]$.

## Chapter 2:

Page/Line Correction
50/4 Should read $\vartheta_{0}+\int_{0}^{t}\left(f g^{\prime}-g f^{\prime}\right) d u$.
50/7 Replace $0_{j}$ by 0 ; (semicolon).
56/17 " $+Y$ ", $Y$ should be italicized.
65/22 $\tilde{\kappa}$, not $\kappa$.
$66 / 4 \quad$ Should read $\sigma=1 / \tau$, not $\sigma=1 / r$
$66 / 7 \quad$ Should read $\gamma=\alpha+\rho N+\rho^{\prime} \sigma B$.
77/22,24 We need simple closed plane curve here and corresponding definition of simple. We also need to know that the curve closes up smoothly (that is, is periodic) in order that statement is true.
83/-10 Should read ...increasing $\vartheta$, not increasing $\varphi$.
85/9 $\quad$ Should read $\omega_{j i}=-\omega_{i j}$.
$86 / 1 \quad$ Should read $\omega_{j i}=-\omega_{i j}$, and $\omega_{j i}(\mathbf{v})=-\omega_{i j}(\mathbf{v})$.
$88 /-2,-1$ In the first matrix, replace " 1 " by " 0 ". In the third matrix, both thetas should be $\vartheta$.
94/-2 $\quad$ Should read $d \rho, \rho \cos \varphi d \vartheta, \rho d \varphi$.
Chapter 3:
Page/Line Correction
102/6 Should read $\mathbf{q}=F(\mathbf{p})$.
116/-6 Insert subscript " $V$ " on left side of equation and italicize $W$.
$121 / 15 \quad \operatorname{In}(2)$, replace $E_{2}$ by $E_{i}$.
121/-1 Each $E_{i}$ should have an overbar.
121/-7 In $F_{i}^{\prime} \cdot F_{j}$, the $F_{\mathrm{s}}$ need to be italicized.

## Chapter 4:

Page/Line Correction
125/7 Should read $\mathbf{R}^{3}$, not $\mathbf{R}^{2}$.
$142 / 9 \quad$ Should read $-1 \leq u \leq 1$, not $-1 \leq v \leq 1$.
172/-11 The first double integral should be an integral over $R$, not $\mathbf{x}$.
172/-9 The formula should be labelled (1), for reference on p. 173.
$176 / 13 \quad$ Should read: ...and $\eta$ is a 2 -form on $N$, then $\int_{\mathbf{x}} F^{*} \eta=\int_{F(\mathbf{x})} \eta$.
177/16 Replace $\phi$ by $\eta$.
177/-7 Replace $\int_{\mathbf{x}} V \ldots$ by $\int_{\partial \mathbf{x}} V \ldots$.
180/17 Replace $Z(\mathbf{p})$ by $U(\mathbf{p})$.
182/5 Should read: $\mathbf{x}(u, v)=v \alpha(a)+(1-v) \alpha(u)$.
187/-17 Replace "Exercise 9" by "Exercise 11".
190/5 In the formula, add the subscripts thus: $p_{3} \mathbf{x}_{u}\left(p_{1}, p_{2}\right)+p_{4} \mathbf{x}_{v}\left(p_{1}, p_{2}\right)$.

## Chapter 5:

Page/Line Correction
195/-3 $\quad Z_{a}$ should read $Z_{\alpha}$.
195/-2 Should read $\left(Z_{\alpha}\right)^{\prime}(0)$.
196/8 Replace $(Z \alpha)^{\prime}(0)$ by $\left(Z_{\alpha}\right)^{\prime}(0)$.
197/-13 Replace $\alpha \nabla_{v} U$ by $a \nabla_{v} U$.
200/11 $\quad f_{y}{ }^{2}$ in denom should be italicized.
200/-9 Should read ( $g_{1}(\mathbf{p}), g_{2}(\mathbf{p}), g_{3}(\mathbf{p})$ ).
205/4 Should read: normal sections of $C$ all...
216/-14 $\quad x(D)$ should be $\mathbf{x}(D)$.
217/13 Last component of $\mathbf{x}_{u u}$ is $\frac{\partial^{2} x_{3}}{\partial u^{2}}$.
220/-1 Should read: $-1 / b^{2} \leq K<0$.
220/12 Should read: $\mathbf{x}_{u u}=(0,0,0)$.
221/1 Should read: The minimum value $K=-1 / b^{2}$ occurs...
223/3 Should read: $f_{u u} f_{v v}-f_{u v}{ }^{2}=0$;
224/9 Should read: $\left(\sqrt{1+x^{2}}, \pm \sqrt{1+y^{2}}, y \sqrt{1+x^{2}} \pm x \sqrt{1+y^{2}}\right)$.
$225 /-4 \quad$ Should read: If $\beta$ is a unit speed curve...
232/20 Should read: ...principal curvature $k_{i}$, not $\kappa_{i}$.
238/-16 The first row of the determinant should read $a_{2}{ }^{\prime 2}-a_{1}{ }^{\prime} a_{2}{ }^{\prime} a_{1}{ }^{\prime 2}$.
243/-5 $\quad h^{\prime 2}$ in denom for $K$ should be italicized.
244/11 Should read: The curve $y=c \cosh (x / c)$, not $(v / c)$.
245/11 Should read: By exercise 2.8, not 2.10.
245/-3 Should read: ...are given in Exs. 5.5 and 6.15.
248/-6 Should read: $\sin \left(a_{*} / c\right)$, not $\sin \left(u_{*} / c\right)$.
248/-5 Should read: $h\left(a_{*}\right)=a \cos \left(a_{*} / c\right)=\ldots$, and $c$ needs to be italicized.

## Chapter 6:

Page/Line Correction
260/7 matrix given is transpose of desired matrix.
266/11 $\quad \mathbf{R}^{3}$ should be bold.
263/-16 Replace "from" with "form".
268/-10 second $V$ in $V[V[f]]$ should be italic.
269/5 Should read: Ex. 2.2(a), not Corollary 2.4.
269/-14 $\quad \mathbf{R}^{3}$ should be bold.
270/-15 Should read: $M \subset \mathbf{R}^{3}$, not $\mathbf{R}^{2}$ and be bold.
270/9 Should read: Ex. 8.14, not Ex. 8.7.
273/10 Warning: In this Lemma $F$ stands for the isometry and coordinate expression for $\mathbf{x}_{u} \cdot \mathbf{x}_{v}$.
286/12 Should read: Ex. 4.8, not Ex. 4.7.
$287 / 3 \quad$ Should read: $\mathbf{x}(u, v)$ to $\mathbf{x}(u, v+\Delta v)$ is approximated by $\Delta v \mathbf{x}_{v}$.
289/9 Should read: ...one set $\mathbf{x}_{i}\left(R_{i}{ }^{\circ}\right)$.
290/5 Should read: ...on any pair of tangent vectors to $M$ is $\pm\|\mathbf{v} \times \mathbf{w}\|$.
291/7 Should read: area $\left(\mathbf{x}_{i}\left(R_{i}\right)\right)$.
294/-7 Should read: Example 7.1 of Chapter 5 (not Example 6.1).
294/-2 Delete $d u d v$.
297/-12 Should read: $G^{*}(d \Sigma)(\mathbf{v}, \mathbf{w})=\ldots$.
302/4 Should read: Ex. 7.6, not Ex. 7.8.
303/-13 Replace $x^{2}+y^{2}$ in the numerator by $x^{2}-y^{2}$.

## Chapter 7:

Page/Line Correction
$313 / 2$ the first subscript on this line should be "2", not "1".
314/11 The expression beneath the square root sign should be: ${a_{1}}^{\prime 2}+{a_{2}}^{\prime 2}$.
315/11 Delete the "2" from the formula.
$320 /-1 \quad$ Should read: $s(t)=\int_{0}^{t} \frac{d u}{1-(u / 2)^{2}}=\ldots$
326/10 Delete two parens "(": one before the first $E_{1}$, the other before the first $E_{2}$.
328/19 What is $J$ ? Rotation operator from Ex. 1.3 of Chapter 7?
332/-9 Should read: ...where $\dot{Y}$ denotes ...
334/-1 Change sign $\ldots-G_{v} a_{2}^{\prime 2}$ to $+G_{v} a_{2}^{\prime 2}$.
$345 / 1 \quad$ Should read: $\cos ^{-1}(c / u)$.
$345 / 7 \quad$ Replace $\mathbf{v}$ by $\mathbf{x}$.
347/19 Should read: Poincaré.
351/-11 Should read: ...but $\kappa_{g}<0$ for a (right turning) clockwise trip.
351/-9 Should read: Corollary 4.6, not Lemma 4.6.
354/5 Should read: ...of $\mathbf{x}$, not $\mathbf{x}_{u}$.
364/-10 Delete "no" from (1).
368/11 The first integral is over the whole manifold $M$, not just the polygonal region.
372/1 Should read Figure 7.26, not Example 7.26.

## Chapter 8:

Page/Line Correction
375/14,17 Should read: arc length.
377/5 Should read: $\gamma_{v}{ }^{\prime}(0)$, not $\gamma_{v}(0)$.
379/-15 Should read: $\exp _{p}$, not $\exp _{v}$.
380/-3 The expression under the square root should read: $a_{1}^{\prime 2}+G a_{2}^{\prime 2}$.
384/4,5 Reletter (b)..(c) as (c)..(d).
385/2,3 (a) should read "...to these geodesics." (b) should read "...curves in (a)."
389/11 Delete the sentence: "Similarly..."
389/-2 Should read: Section 7, not Section 6.
392/4 Should read: $(u \cos v, u \sin v)$.
392/14 Should read: $\sqrt{G}(\pi, v)$.
396/10 Should read: $g^{\prime}(s) \geq 1$.
398/8 Should read: ... $+o\left(\varepsilon^{3}\right)$.
400/8 Should read: (Ch. 4, Sec. 2).
402/-2 The $N$ should be $\tilde{M}$ as in the Proposition.
410/15 Should read: Hopf-Rinow theorem (2.1), not (2.2).
416/9 Should read: $\ldots=\left(x^{2} / \sqrt{2}, y^{2} / \sqrt{2}, z^{2} / \sqrt{2}, \ldots\right)$.
426/-14,-13 Replace larger by smaller and longer by shorter, also Fig. 6.8, not 6.9.
426/-6 Should read: $4 \pi / k$.

## Answers:

Page/Line Correction
451/1 Should read: $y^{3}$.
451/6 Should read: $\alpha^{\prime}(\pi / 2)=(-1,0,1 / \sqrt{2})_{p}$, where $p=(1,1, \sqrt{2})$.
469/5 Replace $\omega_{13}(Y) E_{3}$ by $\omega_{12}(Y) E_{3}$ and subscript " $y$ " by " $Y$ ".
474/-5 Should read: Lemma 7.4, not 7.3.

## Index:

Page/Line Correction
481/24 (right col) Should read: ...Surface of revolution, 130, 241-250, not 234-242.
481/26 (left col) Should read: ...Smooth disk, 185, (Ex. 6), not Ex.5.

Figures:
Also, on p. 35, replace Fig. 1.14-a duplicate of Fig. 1.13 by


